

Non-stationary analysis of extreme precipitation

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Bridging the gap between water science and solutions – A joint conference

9th IWRM **14th STAHY** **1st EBHE**



The Guardian

Afghanistan flash floods kill more than 300 as torrents of water and mud crash through villages

Survivors pick through debris-littered streets and damaged buildings as rescue workers dispatched amid warning some areas cut off by flooding



Europe hit by severe floods in the north and heatwaves in the south

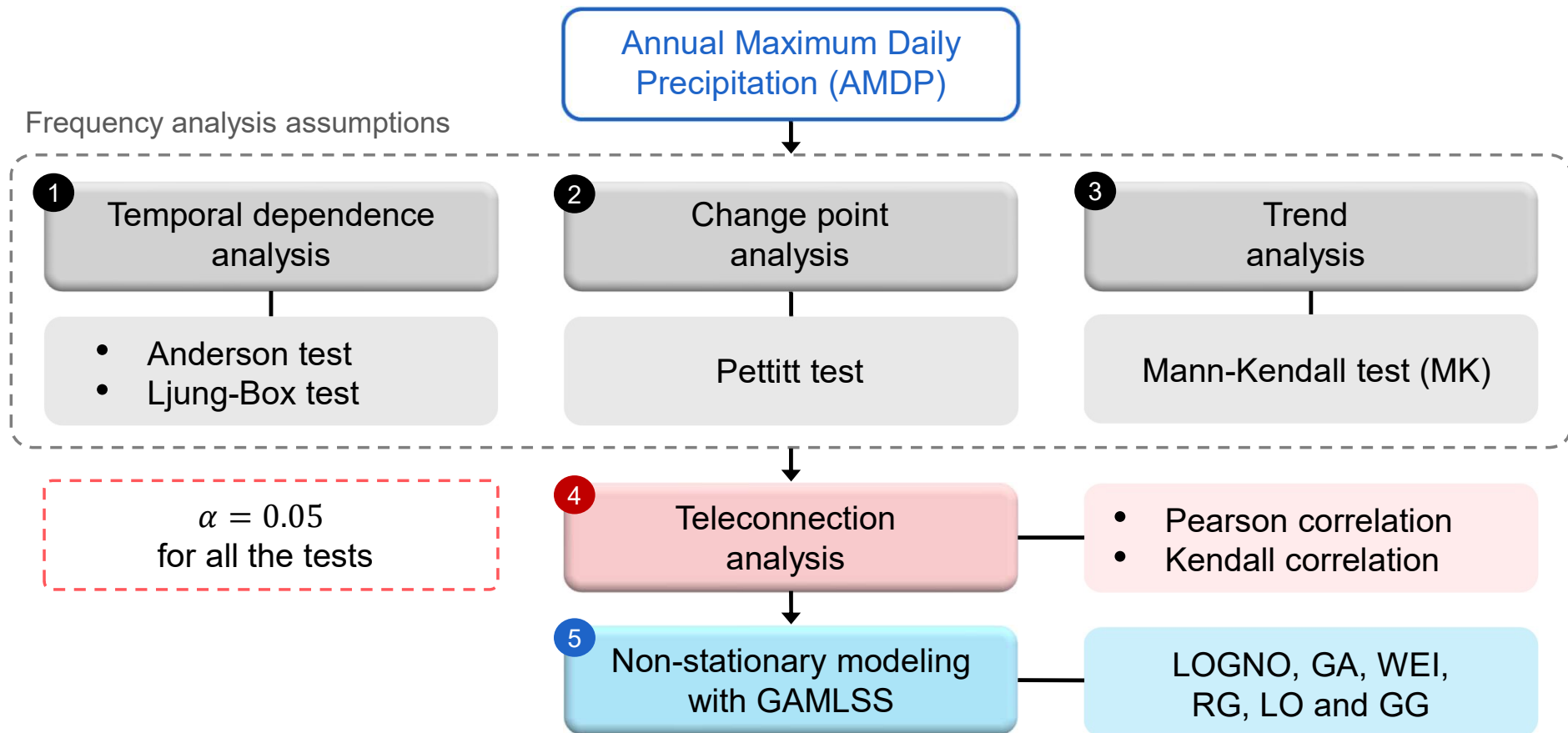


- Research question:

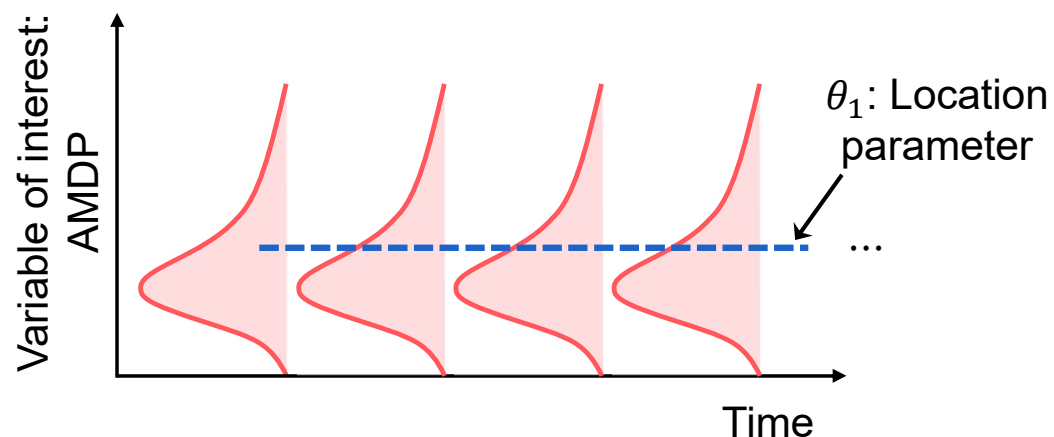
Are extreme precipitations in Spain experiencing any deviation from the stationary assumption that makes it necessary to consider a non-stationary frequency analysis?

- Objective:

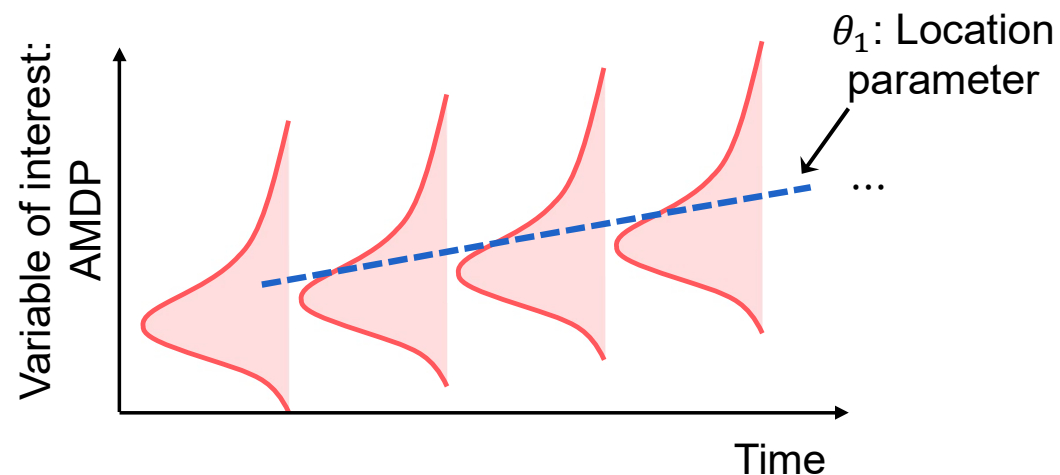
Analyze the frequencies of Annual Maximum Daily Precipitation (AMDP) over Spain through a non-stationary approach and make predictions under climate change scenarios



Conventional frequency analysis (stationary)



Non-stationary frequency analysis



Generalized Additive Models for Location, Scale and Shape (Rigby & Stasinopoulos, 2005)

Semi-parametric additive model:

$$g_k(\theta_k) = X_k\beta_k + \sum_{j=1}^{m_j} h_{jk}(x_{jk})$$

Probability distribution with three parameters:

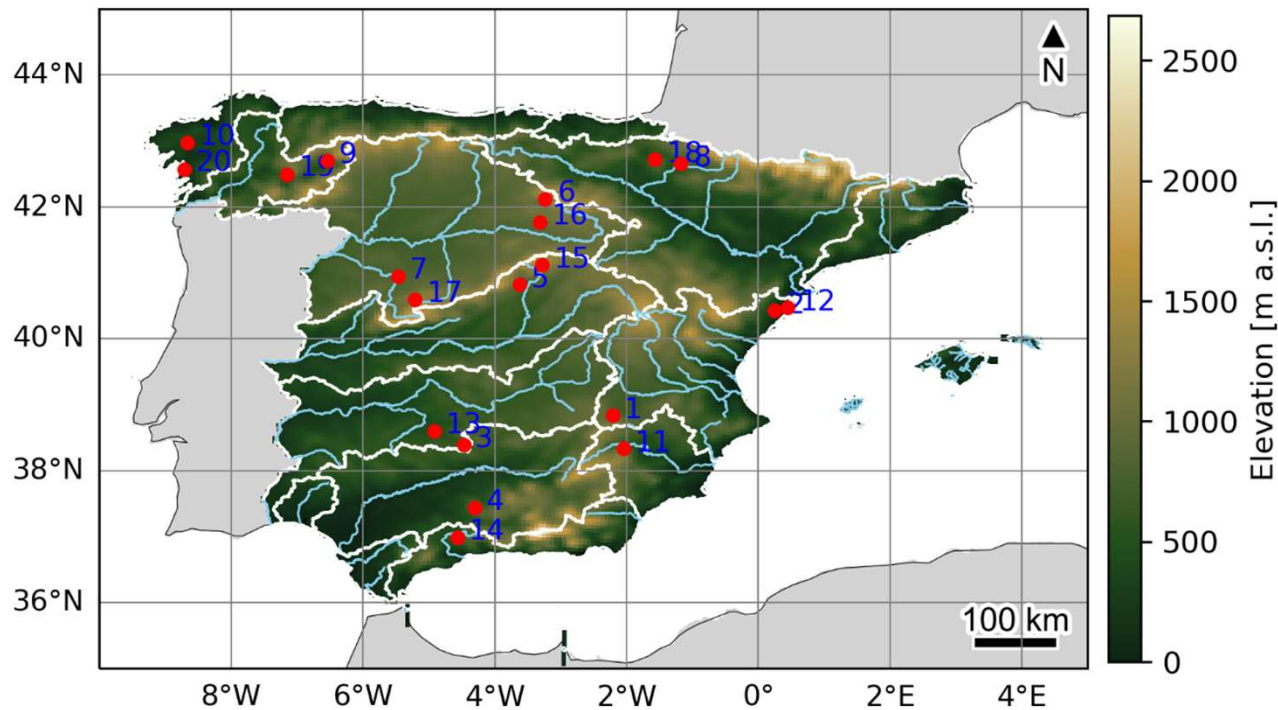
$$\begin{aligned} g_1(\theta_1) &= X_1\beta_1 + \sum_{j=1}^{m_1} h_{j1}(x_{j1}) \\ g_2(\theta_2) &= X_2\beta_2 + \sum_{j=1}^{m_2} h_{j2}(x_{j2}) \\ g_3(\theta_3) &= X_3\beta_3 + \sum_{j=1}^{m_3} h_{j3}(x_{j3}) \end{aligned}$$

$g_k(\cdot)$ is the link function (e.g., identity, logarithmic)

$X_k\beta_k$ is the parametric linear component

$h_{jk}(\cdot)$ represents the functional dependence of the distribution parameters on covariates x_{jk} ; it can be linear or non-linear through smoothing terms (cubic splines were used in this study)

Peninsular Spain and Balearic islands



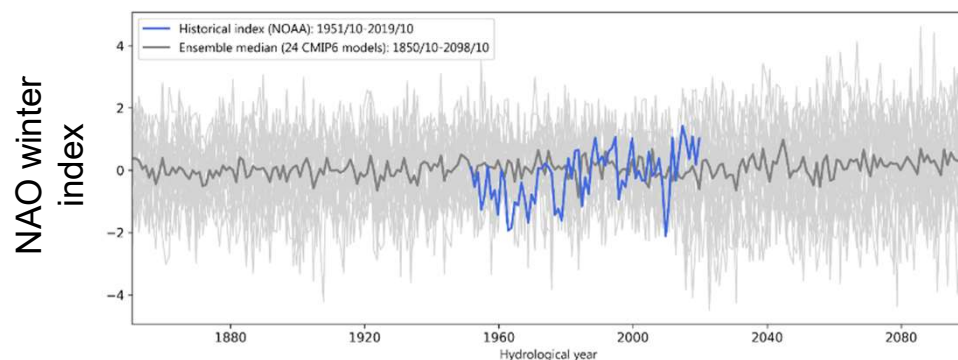
Precipitation data

- Gridded dataset by AEMET
- Spatial resolution: $0.05^\circ \times 0.05^\circ$ ($\sim 5 \text{ km} \times 5 \text{ km}$; 16 156 grid points)
- Temporal resolution: daily
- Temporal coverage: 1/1/1951-31/12/2020 (70 calendar years)

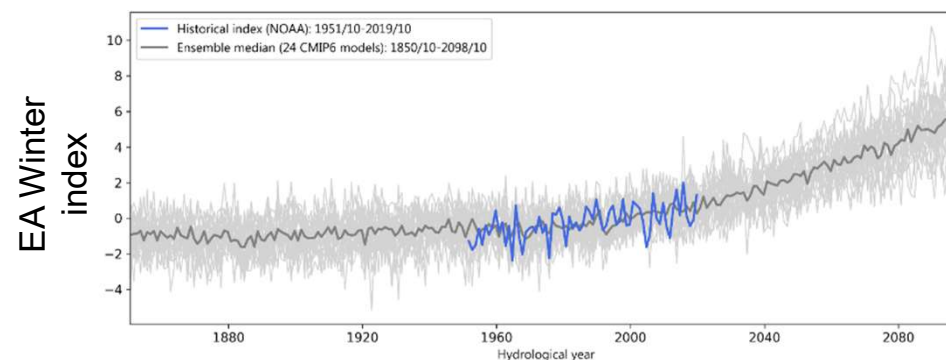
Winter climate indices data

- Historical: CPC-NOAA (USA)
- Future: Cusinato et al. (2021) 24 climate models (CMIP6) / ssp585

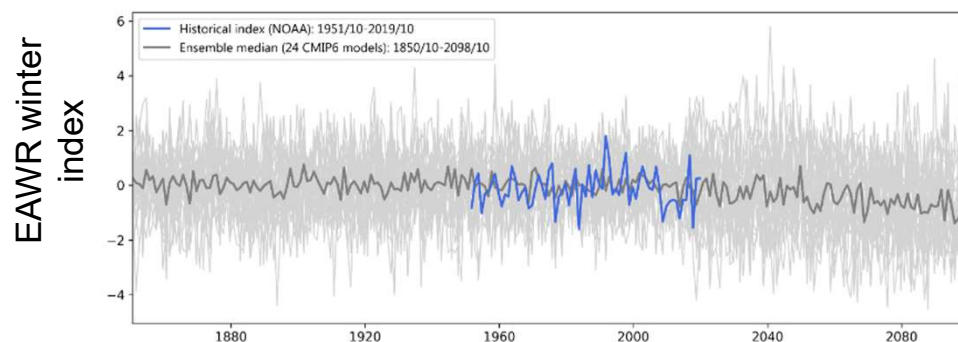
North Atlantic Oscillation (NAO) index



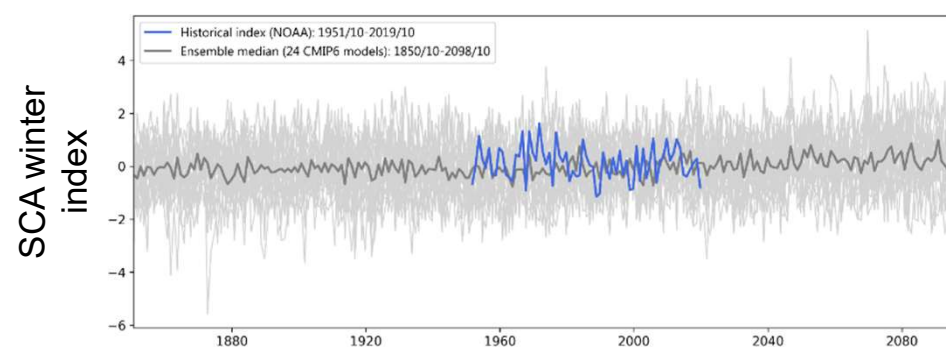
East Atlantic (EA) index



East Atlantic-Western Russia (EAWR) index

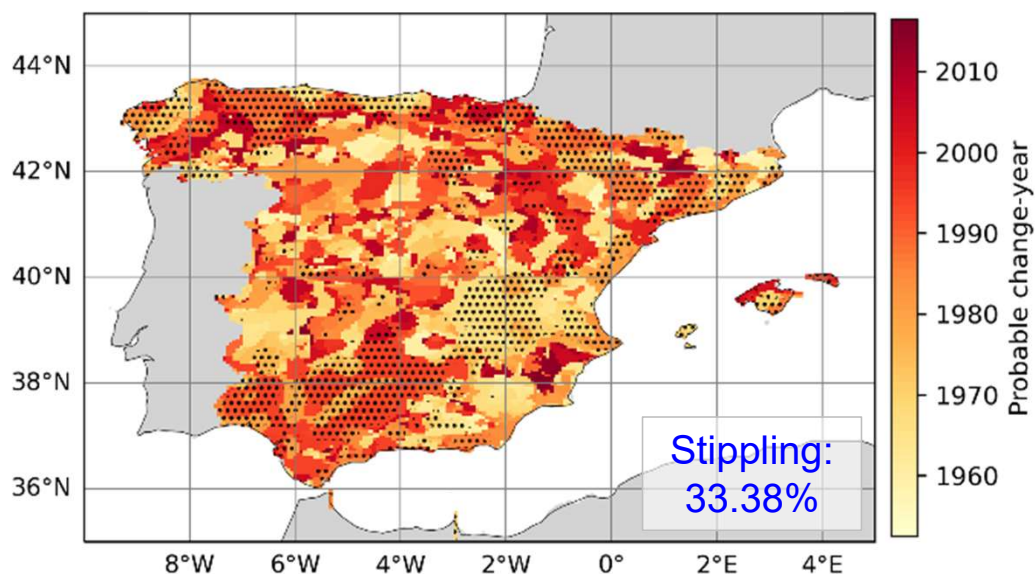


Scandinavian (SCA) index



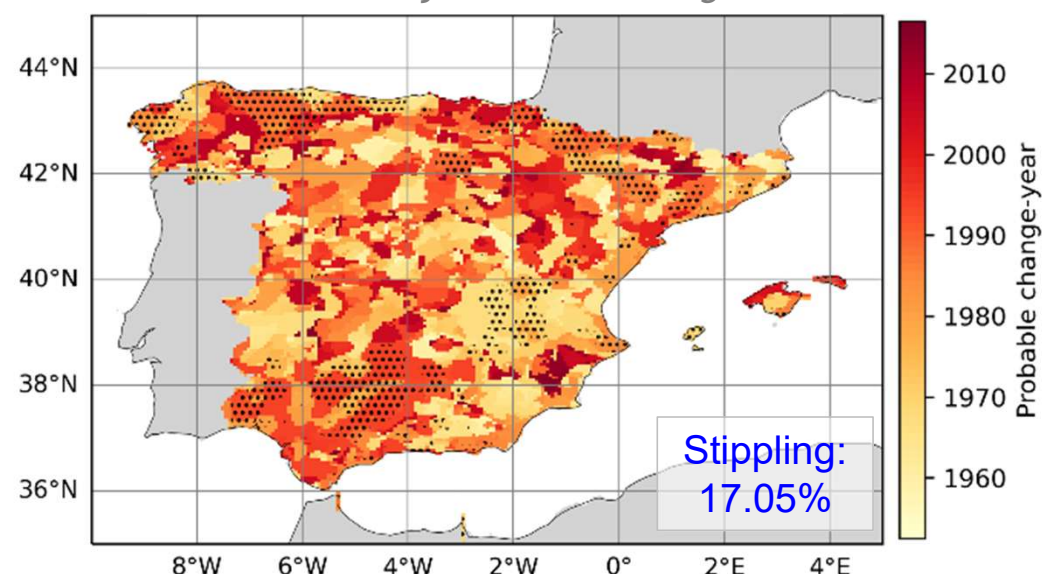
Pettitt test

Local evaluation



Global evaluation

FDR - Benjamini & Hochberg



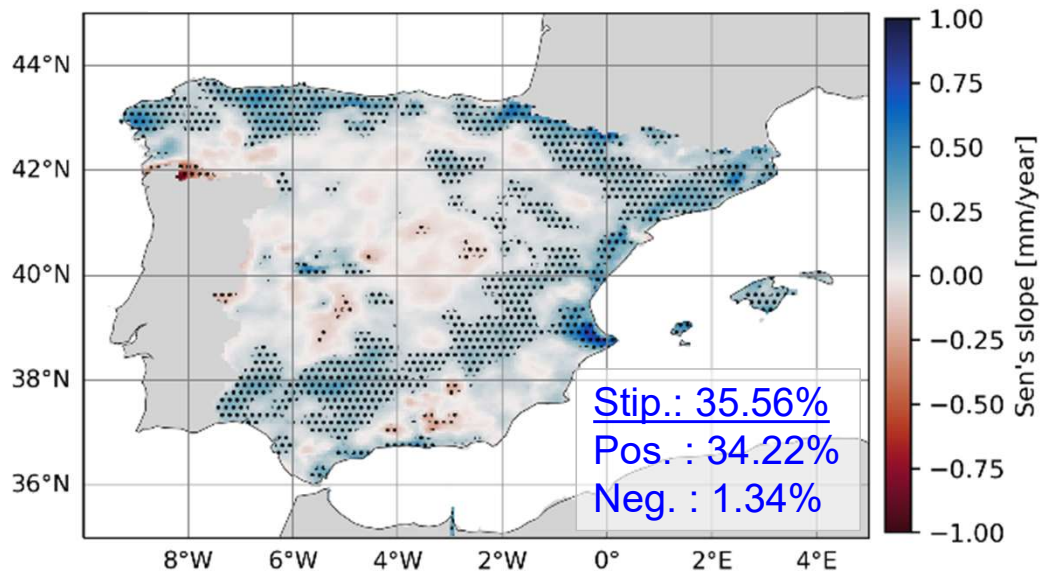
Effect of test multiplicity



Reduction of significant results

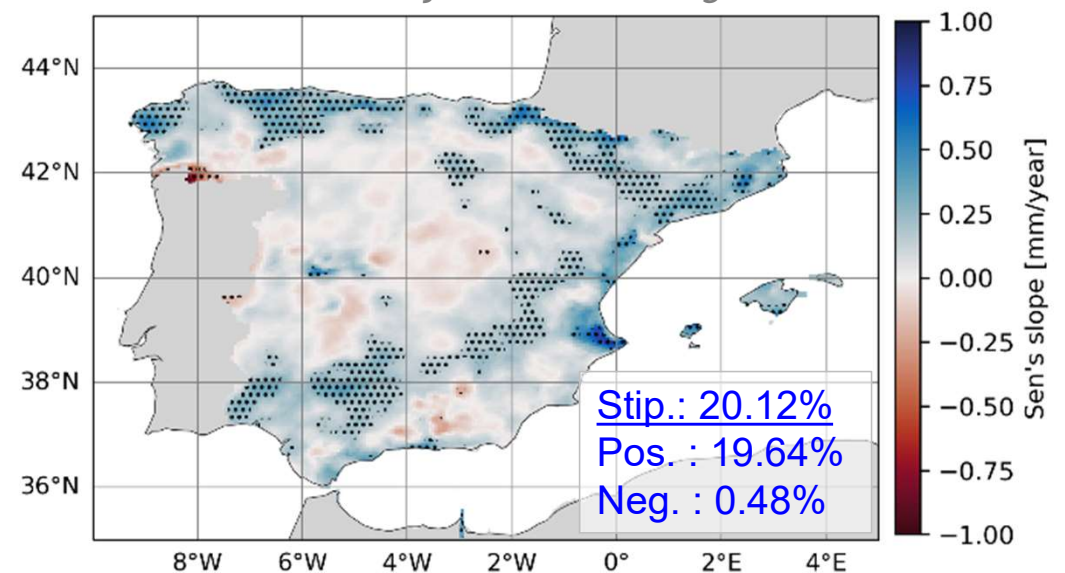
Mann-Kendall test

Local evaluation



Global evaluation

FDR - Benjamini & Hochberg



Effect of test multiplicity

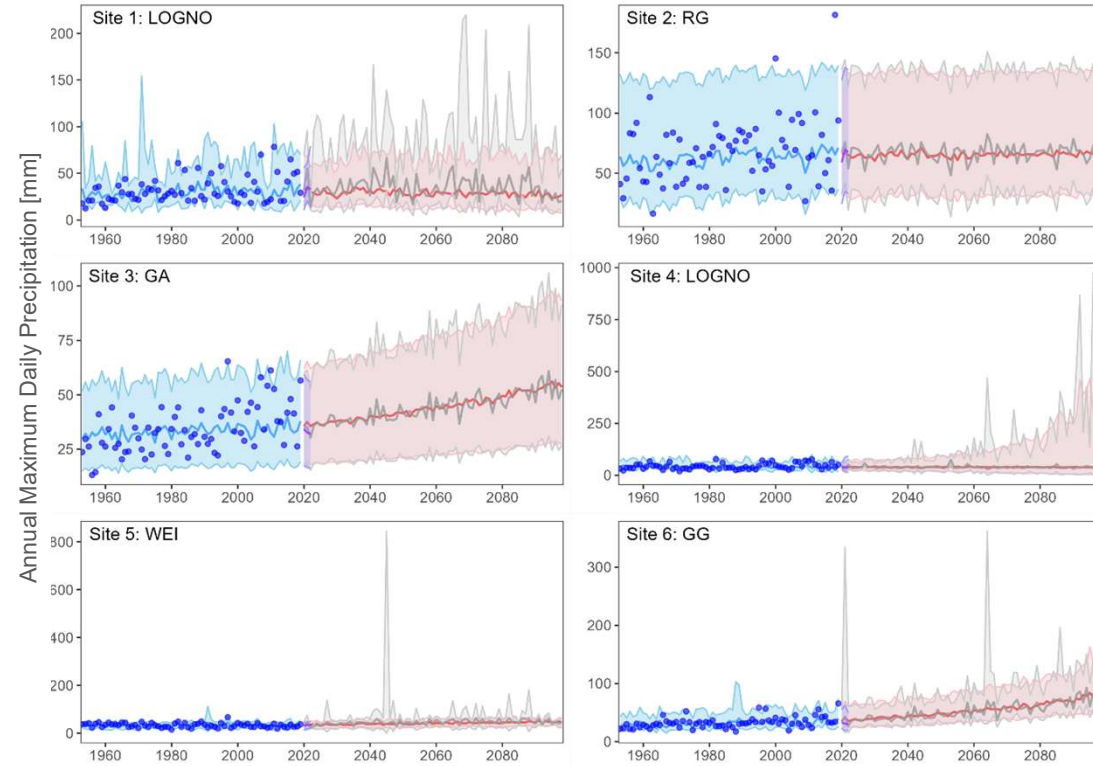
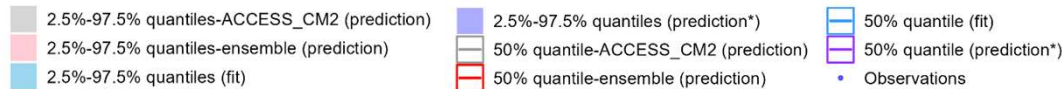


Reduction of significant results

Series of 20 sites were modeled

Site	PDF	AIC-S	AIC-NS	DF	Par.	Model structure
1	LOGNO	528.421	511.639	6	θ_1 θ_2	$3.434 + 0.155 \cdot NAOw + 0.222 \cdot EAWRw$ $-1.089 + 0.498 \cdot SCAw + 0.308 \cdot NAOw$
2	RG	626.705	623.282	3	θ_1 θ_2	$56.896 + 6.606 \cdot NAOw$ 3.027
3	GA	509.627	507.384	3	θ_1 θ_2	$3.553 + 0.086 \cdot EAw$ -1.180
4	LOGNO	539.202	522.229	10	θ_1 θ_2	$3.703 + cs(NAOw, 2)$ $-1.327 + cs(EAw, 3) + 0.277 \cdot NAOw$
5	WEI	494.420	472.068	11	θ_1 θ_2	$3.607 + cs(EAw, 3) + 0.193 \cdot EAWRw$ $1.623 + cs(EAWRw, 3)$
6	GG	483.709	467.206	7	θ_1 θ_2 θ_3	$3.443 + 0.155 \cdot EAw$ $-1.518 + cs(SCAw, 2)$ -1.962

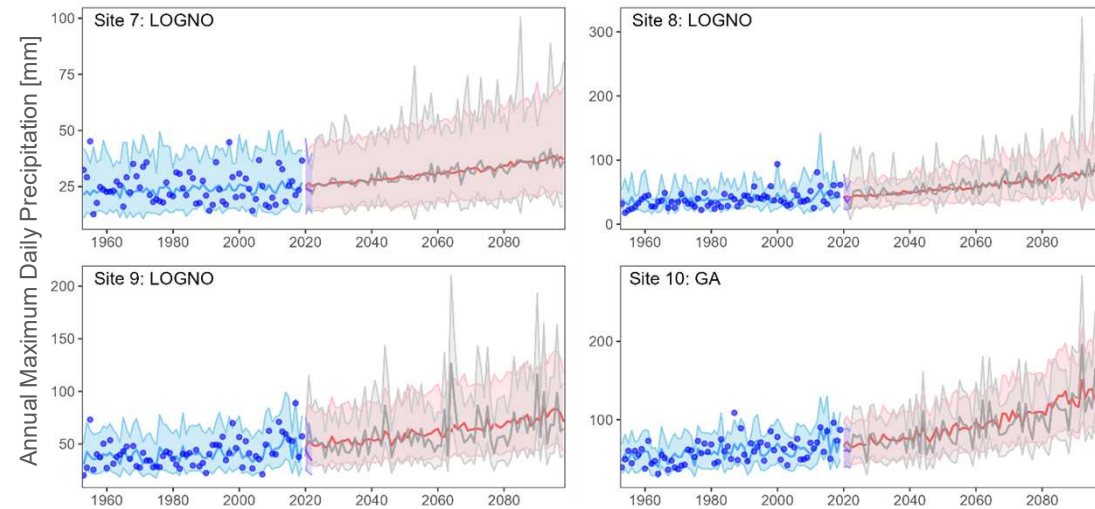
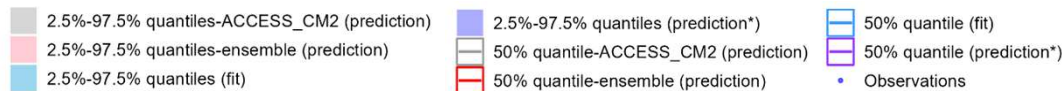
Legend



Sudden increases and decreases in variance

Site	PDF	AIC-S	AIC-NS	DF	Par.	Model structure
7	LOGNO	449.596	447.669	4	θ_1 θ_2	$3.180 + 0.081 \cdot EAw$ $-1.339 + 0.239 \cdot SCAw$
8	LOGNO	520.824	500.781	10	θ_1 θ_2	$3.665 + 0.113 \cdot EAw + 0.163 \cdot SCAw$ $+ 0.091 \cdot NAOw$ $-1.490 - 0.391 \cdot EAWRw + cs(SCAw, 3)$
9	LOGNO	531.261	522.387	10	θ_1 θ_2	$3.688 + cs(NAOw, 3) + cs(EAWRw, 2)$ $+ 0.078 \cdot EAw$ -1.353
10	GA	557.921	530.475	5	θ_1 θ_2	$4.111 + 0.122 \cdot EAw + 0.093 \cdot NAOw$ $- 0.114 \cdot EAWRw$ -1.600

Legend



The scale parameter covariates took values at the limits and outside their historical range

Extrapolation

Origin?



Combined effects

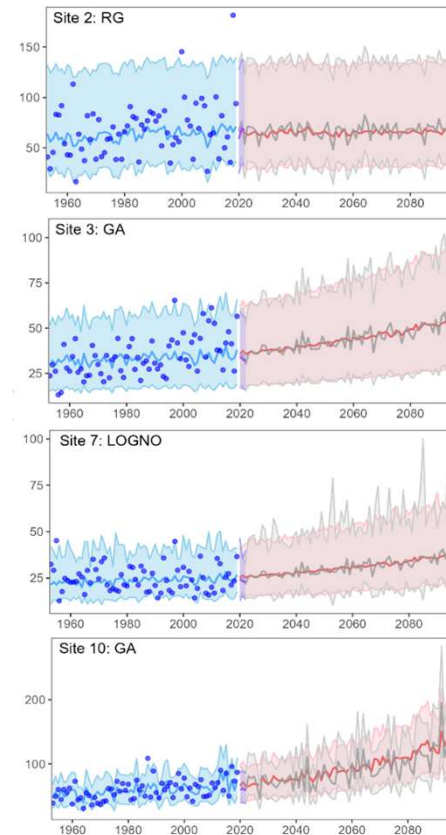
Maximization/minimization of the variance

Results: non-stationary modeling, lagged covar.

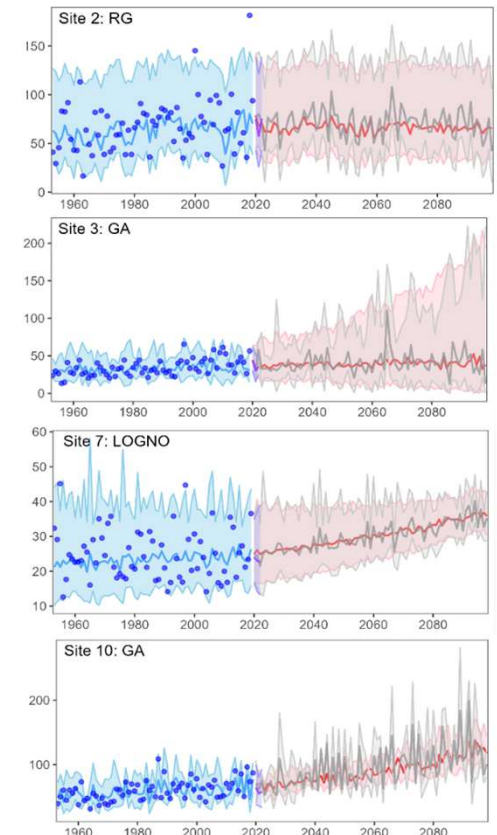
Site	PDF	AIC-S	AIC-NS	DF	Par.	Model structure
2	RG	626.705	615.604	4	θ_1 θ_2	$59.761 + 11.321 \cdot NAOw_1 + 5.937 \cdot EAWRw$ 2.956
3	GA	509.627	500.219	10	θ_1 θ_2	$3.550 + 0.096 \cdot EAw_1 - 0.176 \cdot SCAw_1$ $+ cs(NAOw_1, 3)$ $-1.367 - 0.355 \cdot NAOw_1 + 0.242 \cdot EAw$
7	LOGNO	449.596	445.722	4	θ_1 θ_2	$3.170 + 0.077 \cdot EAw$ $-1.378 - 0.223 \cdot EAw_1$
10	GA	557.921	516.951	14	θ_1 θ_2	$4.118 + 0.129 \cdot EAw + 0.056 \cdot NAOw$ $- 0.094 \cdot EAWRw + 0.154$ $\cdot EAWRw_1$ $-1.900 + cs(EAWRw, 3) + cs(NAOw, 3)$

- Models with lagged covariates have higher performance than models with non-lagged covariates, but their complexity also increases
- High sensitivity of models in the predictive phase

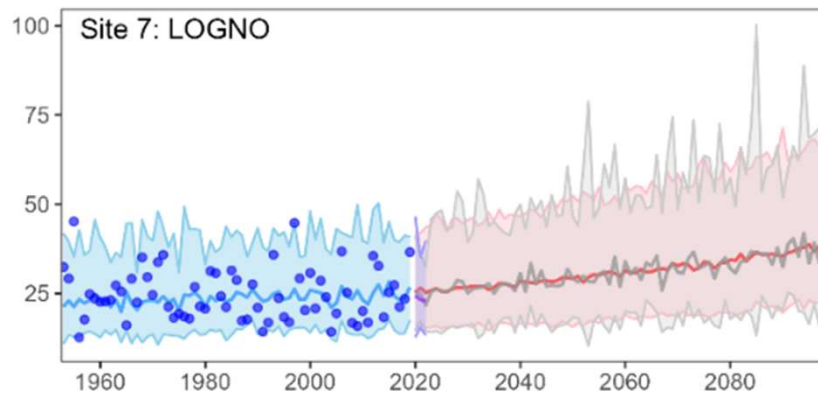
Non-lagged covariates



Lagged-1 covariates

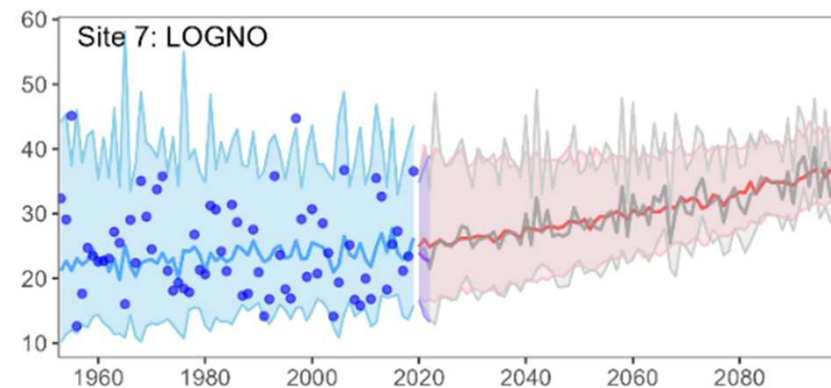


Non-lagged covariates



Site	PDF	AIC-S	AIC-NS	DF	Par.	Model structure
7	LOGNO	449.596	447.669	4	θ_1	$3.180 + 0.081 \cdot EAw$
					θ_2	$-1.339 + 0.239 \cdot SCAw$
7	LOGNO	449.596	445.722	4	θ_1	$3.170 + 0.077 \cdot EAw$
					θ_2	$-1.378 - 0.223 \cdot EAw_1$

Lagged-1 covariates



- Different model structures (see θ_2)
- Similar AIC
- Opposite behavior in projected variance (?)

Which model do I select?  Equifinality

- ❑ AMDP over several Spanish regions are experiencing some deviation from the stationary assumption (change points and trends)
- ❑ Non-stationary modeling revealed serious problems that led to doubts about the reliability of the adopted models
 - Equifinality makes it difficult to select a representative non-stationary model
 - There is uncertainty associated with extrapolating the relationships between distribution parameters and covariates into the future, as these relationships may change as the sample data increase
- ❑ There are no projections for all climate indices
- ❑ **We need to find a physical mechanism to explain non-stationarities**

Thank you for your attention!

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