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# Non-stationary analysis of extreme precipitation

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Bridging the gap between water science and solutions – A joint conference

9<sup>th</sup> IWRM 14<sup>th</sup> STAHY 1<sup>st</sup> EBHE



## The Guardian

Afghanistan flash floods kill more than 300 as torrents of water and mud crash through villages

Survivors pick through debris-littered streets and damaged buildings as rescue workers dispatched amid warning some areas cut off by flooding



## Europe hit by severe floods in the north and heatwaves in the south



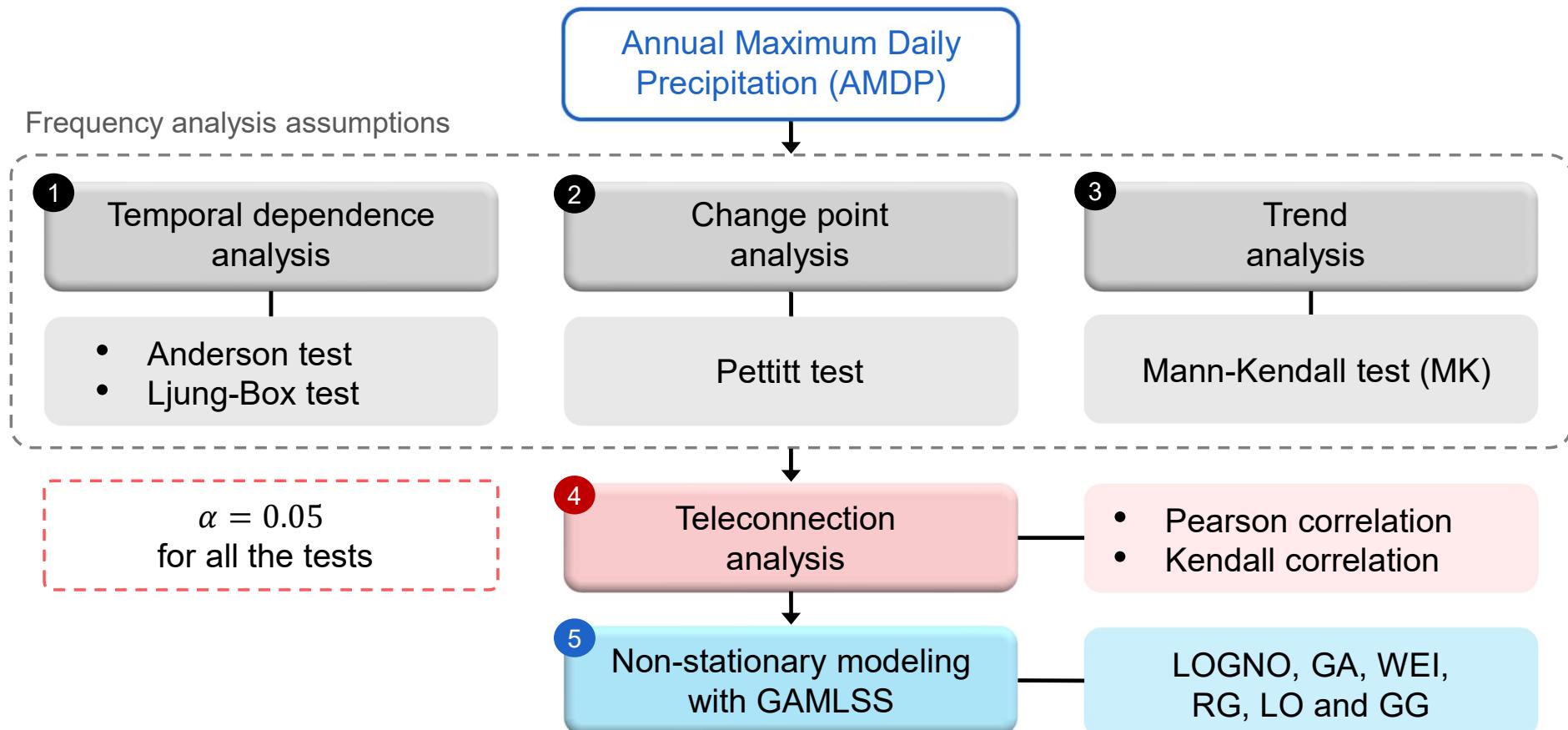
## Research question and objective

- Research question:

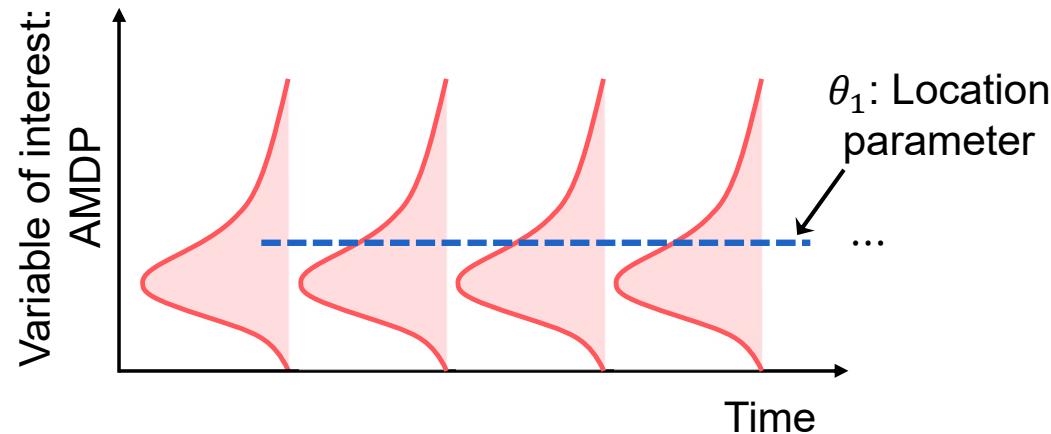
Are extreme precipitations in Spain experiencing any deviation from the stationary assumption that makes it necessary to consider a non-stationary frequency analysis?

- Objective:

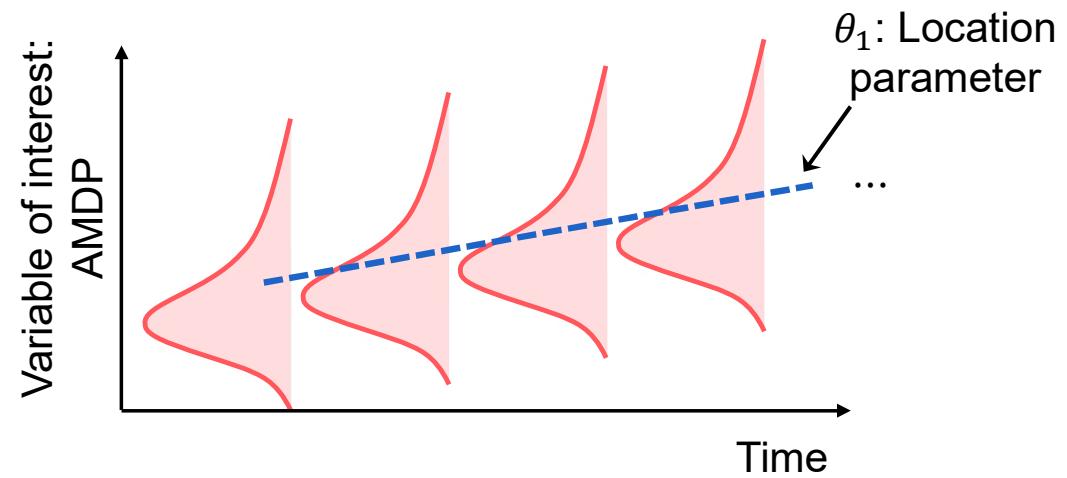
Analyze the frequencies of Annual Maximum Daily Precipitation (AMDP) over Spain through a non-stationary approach and make predictions under climate change scenarios



## Conventional frequency analysis (stationary)



## Non-stationary frequency analysis



## Generalized Additive Models for Location, Scale and Shape (Rigby & Stasinopoulos, 2005)

Semi-parametric additive model:

$$g_k(\theta_k) = X_k \beta_k + \sum_{j=1}^{m_j} h_{jk}(x_{jk})$$

Probability distribution with three parameters:

$$g_1(\theta_1) = X_1 \beta_1 + \sum_{j=1}^{m_1} h_{j1}(x_{j1})$$

$$g_2(\theta_2) = X_2 \beta_2 + \sum_{j=1}^{m_2} h_{j2}(x_{j2})$$

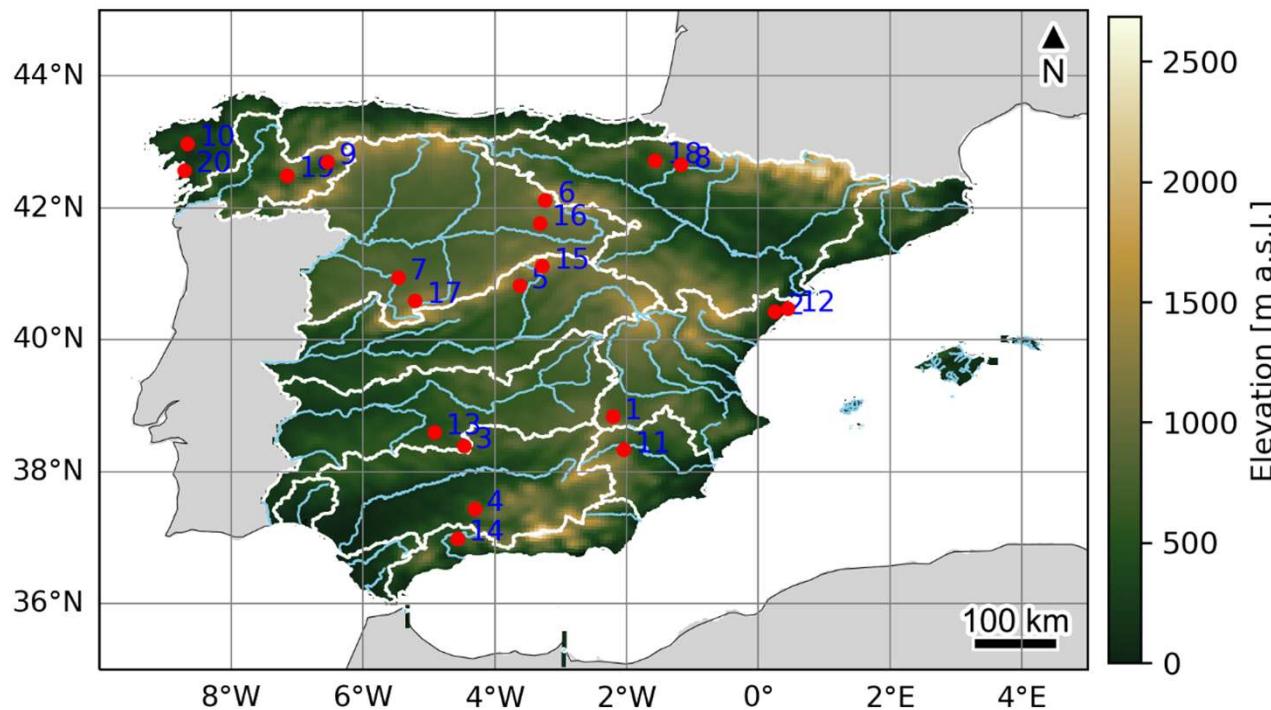
$$g_3(\theta_3) = X_3 \beta_3 + \sum_{j=1}^{m_3} h_{j3}(x_{j3})$$

$g_k(\cdot)$  is the link function (e.g., identity, logarithmic)

$X_k \beta_k$  is the parametric linear component

$h_{jk}(\cdot)$  represents the functional dependence of the distribution parameters on covariates  $x_{jk}$ ; it can be linear or non-linear through smoothing terms (cubic splines were used in this study)

## Peninsular Spain and Balearic islands



## Precipitation data

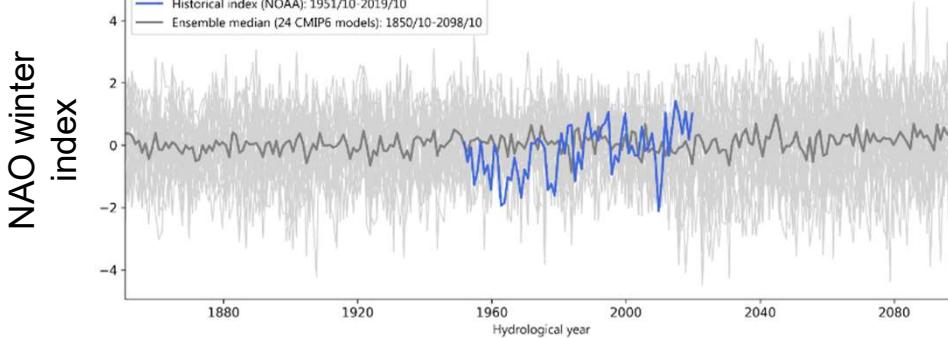
- Gridded dataset by AEMET
- Spatial resolution:  $0.05^\circ \times 0.05^\circ$  ( $\sim 5 \text{ km} \times 5 \text{ km}$ ; 16 156 grid points)
- Temporal resolution: daily
- Temporal coverage: 1/1/1951-31/12/2020 (70 calendar years)

## Winter climate indices data

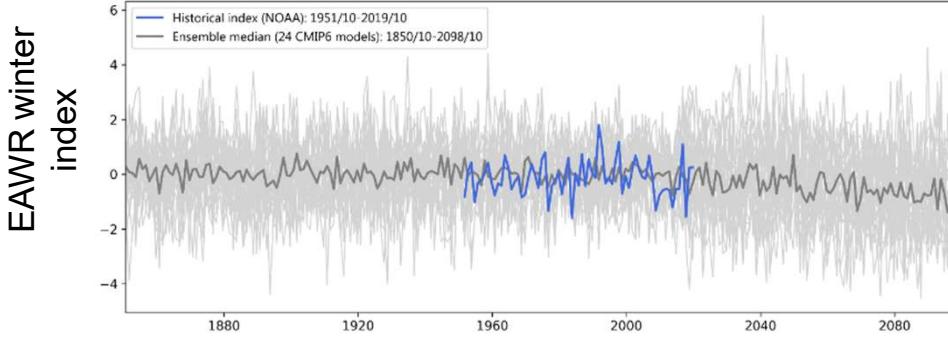
- Historical: CPC-NOAA (USA)
- Future: Cusinato et al. (2021)  
24 climate models (CMIP6) / ssp585

# Historical and projected winter climate indices

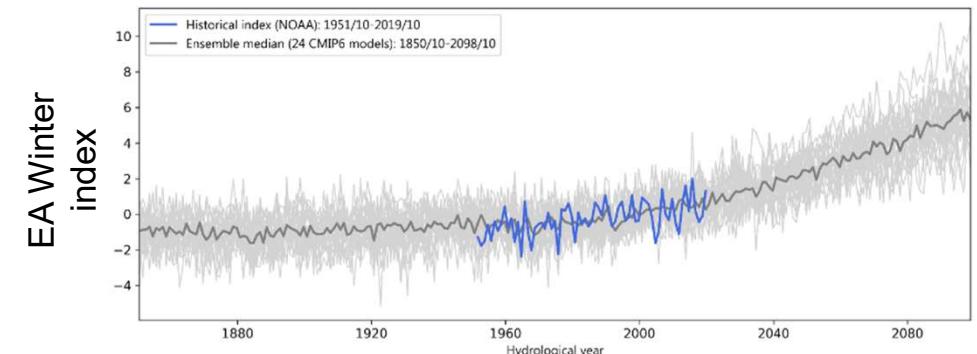
## North Atlantic Oscillation (NAO) index



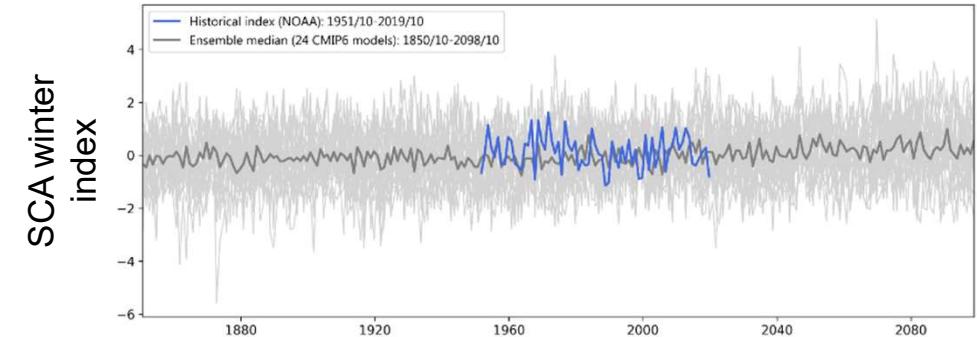
## East Atlantic-Western Russia (EAWR) index



## East Atlantic (EA) index



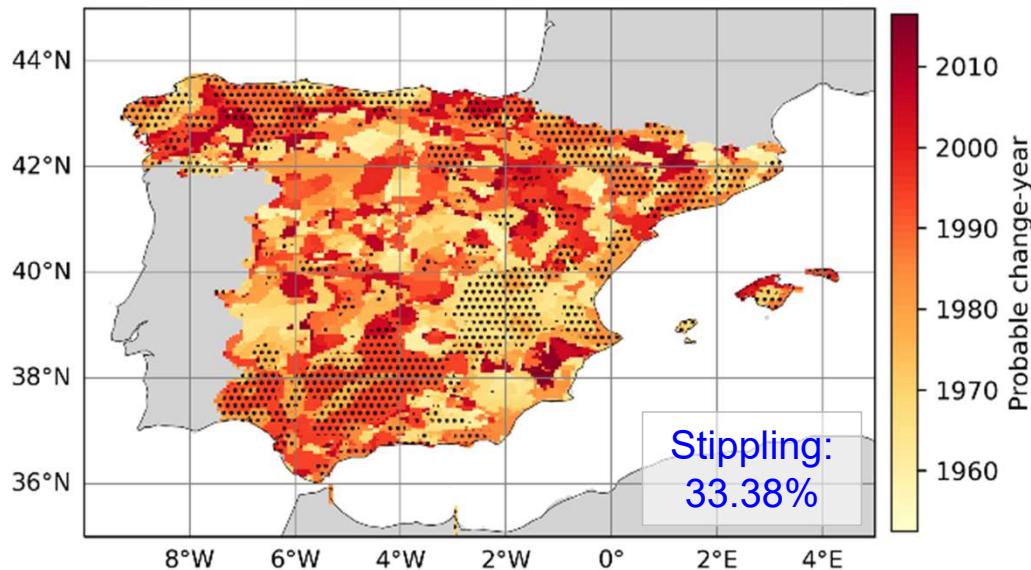
## Scandinavian (SCA) index



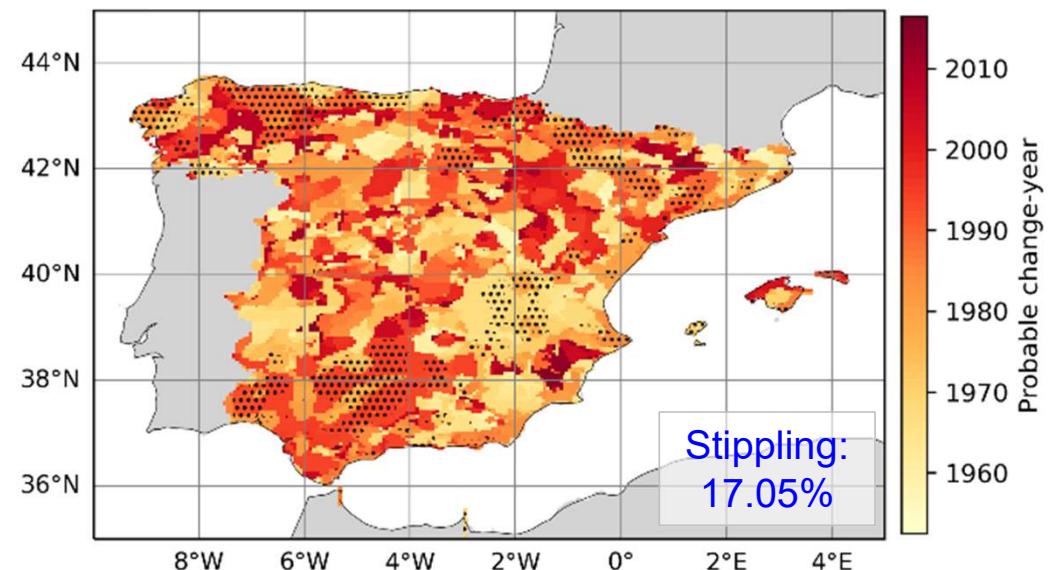
# Results: change points

## Pettitt test

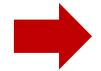
Local evaluation



Global evaluation  
FDR - Benjamini & Hochberg



Effect of test multiplicity

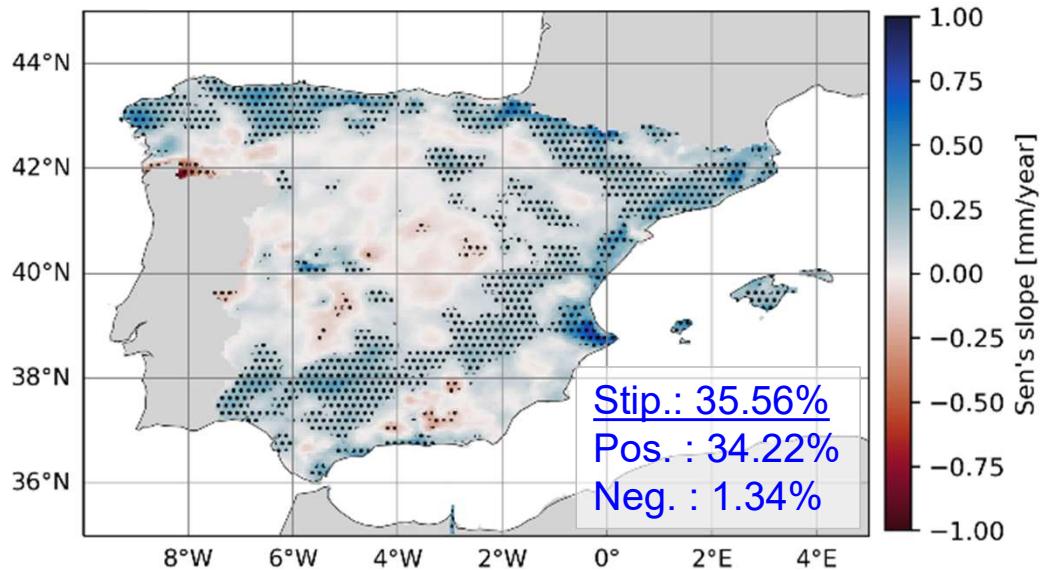


Reduction of significant results

# Results: monotonic trends

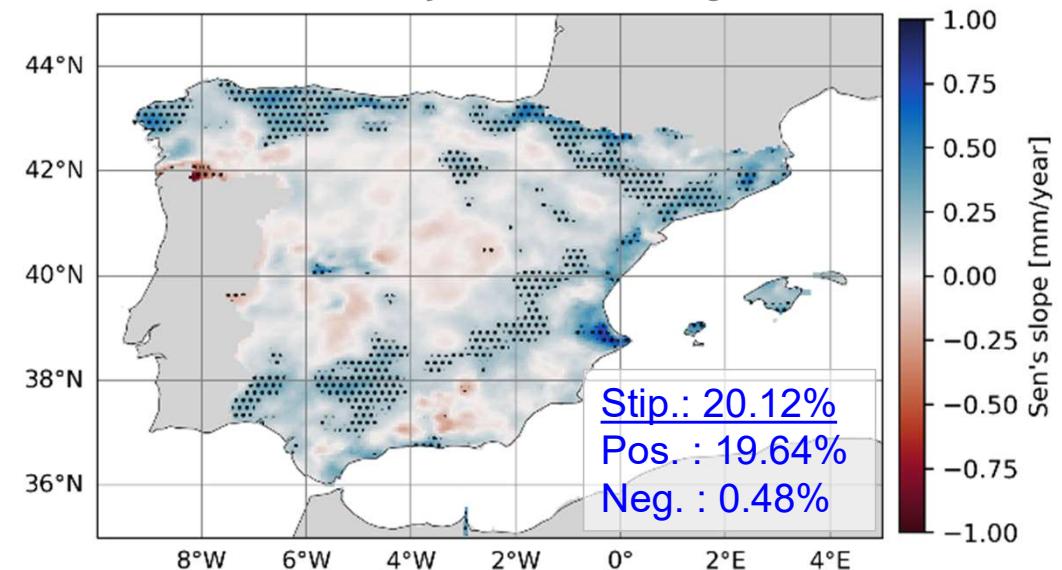
## Mann-Kendall test

### Local evaluation

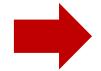


### Global evaluation

*FDR - Benjamini & Hochberg*



Effect of test multiplicity



Reduction of significant results

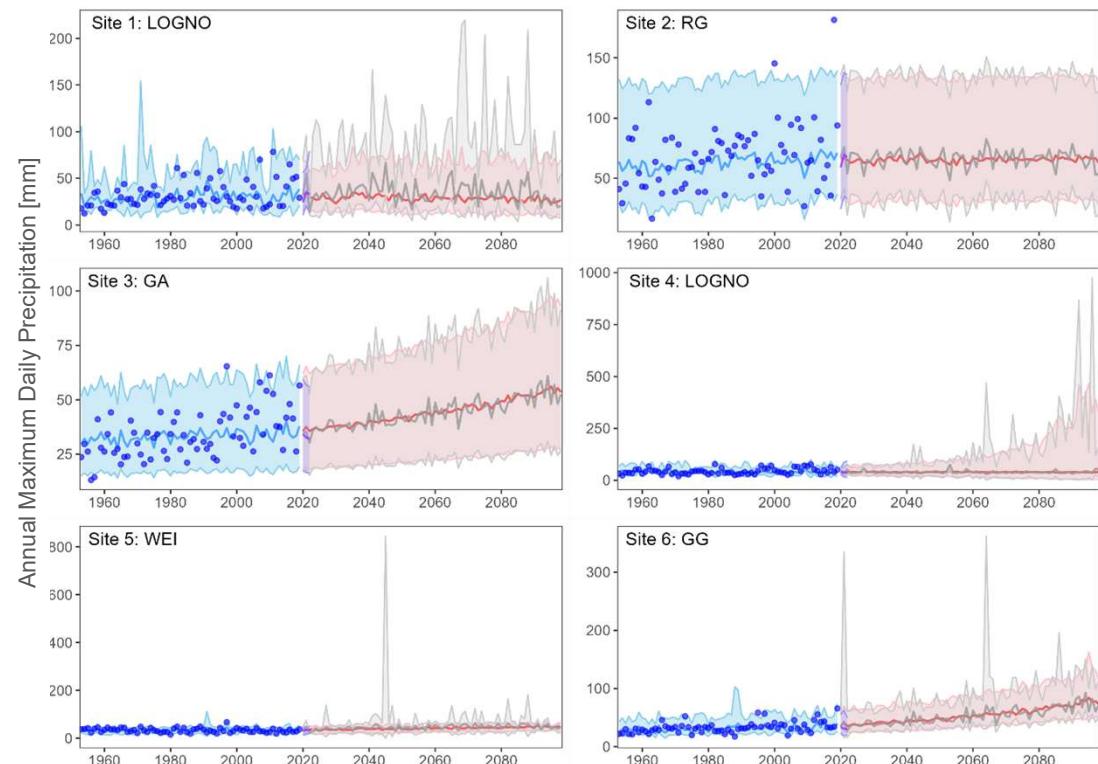
# Results: non-stationary modeling, non-lagged covar.

Series of 20 sites were modeled

Site	PDF	AIC-S	AIC-NS	DF	Par.	Model structure
1	LOGNO	528.421	511.639	6	$\theta_1$	$3.434 + 0.155 \cdot NAOw + 0.222 \cdot EAWRw$
					$\theta_2$	$-1.089 + 0.498 \cdot SCAw + 0.308 \cdot NAOw$
2	RG	626.705	623.282	3	$\theta_1$	$56.896 + 6.606 \cdot NAOw$
					$\theta_2$	3.027
3	GA	509.627	507.384	3	$\theta_1$	$3.553 + 0.086 \cdot EAw$
					$\theta_2$	-1.180
4	LOGNO	539.202	522.229	10	$\theta_1$	$3.703 + cs(NAOw, 2)$
					$\theta_2$	$-1.327 + cs(EAw, 3) + 0.277 \cdot NAOw$
5	WEI	494.420	472.068	11	$\theta_1$	$3.607 + cs(EAw, 3) + 0.193 \cdot EAWRw$
					$\theta_2$	$1.623 + cs(EAWRw, 3)$
6	GG	483.709	467.206	7	$\theta_1$	$3.443 + 0.155 \cdot EAw$
					$\theta_2$	$-1.518 + cs(SCAw, 2)$
					$\theta_3$	-1.962

## Legend

2.5%-97.5% quantiles-ACCESS_CM2 (prediction)	2.5%-97.5% quantiles (prediction*)	50% quantile (fit)
2.5%-97.5% quantiles-ensemble (prediction)	50% quantile-ACCESS_CM2 (prediction)	50% quantile (prediction*)
2.5%-97.5% quantiles (fit)	50% quantile-ensemble (prediction)	• Observations



Sudden increases and decreases in variance

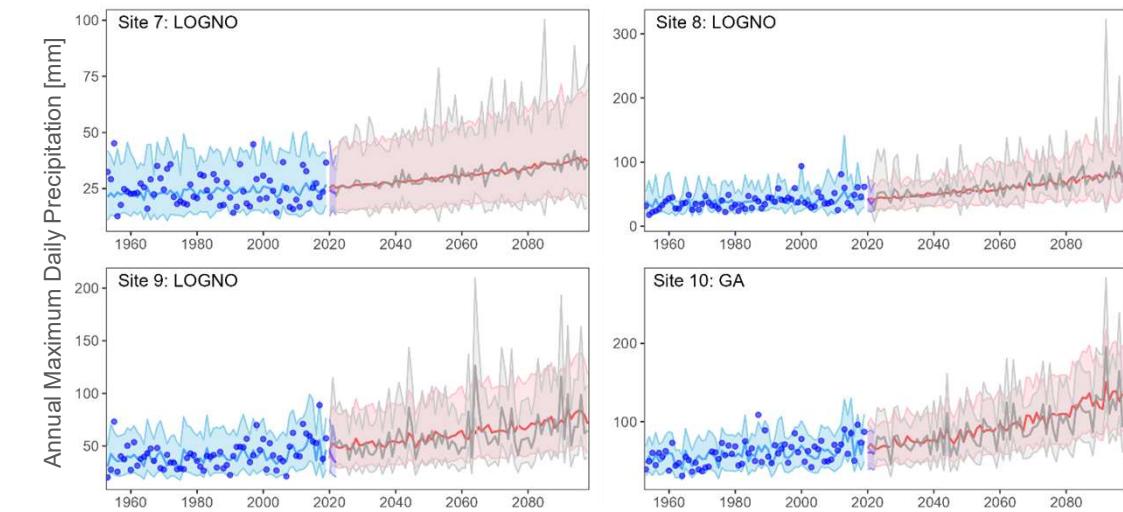
# Results: non-stationary modeling, non-lagged covar.

Site	PDF	AIC-S	AIC-NS	DF	Par.	Model structure
7	LOGNO	449.596	447.669	4	$\theta_1$	$3.180 + 0.081 \cdot EAw$
					$\theta_2$	$-1.339 + 0.239 \cdot SCAw$
8	LOGNO	520.824	500.781	10	$\theta_1$	$3.665 + 0.113 \cdot EAw + 0.163 \cdot SCAw$ + 0.091 $\cdot NAOw$
					$\theta_2$	$-1.490 - 0.391 \cdot EAWRw + cs(SCAw, 3)$
9	LOGNO	531.261	522.387	10	$\theta_1$	$3.688 + cs(NAOw, 3) + cs(EAWRw, 2)$ + 0.078 $\cdot EAw$
					$\theta_2$	-1.353
10	GA	557.921	530.475	5	$\theta_1$	$4.111 + 0.122 \cdot EAw + 0.093 \cdot NAOw$ - 0.114 $\cdot EAWRw$
					$\theta_2$	-1.600

## Legend

- 2.5%-97.5% quantiles-ACCESS\_CM2 (prediction)
- 2.5%-97.5% quantiles-ensemble (prediction)
- 2.5%-97.5% quantiles (fit)
- 50% quantile-ACCESS\_CM2 (prediction)
- 50% quantile (prediction\*)
- 50% quantile (fit)
- Observations

## Extrapolation



The scale parameter covariates took values at the limits and outside their historical range

Origin?



Maximization/minimization of the variance

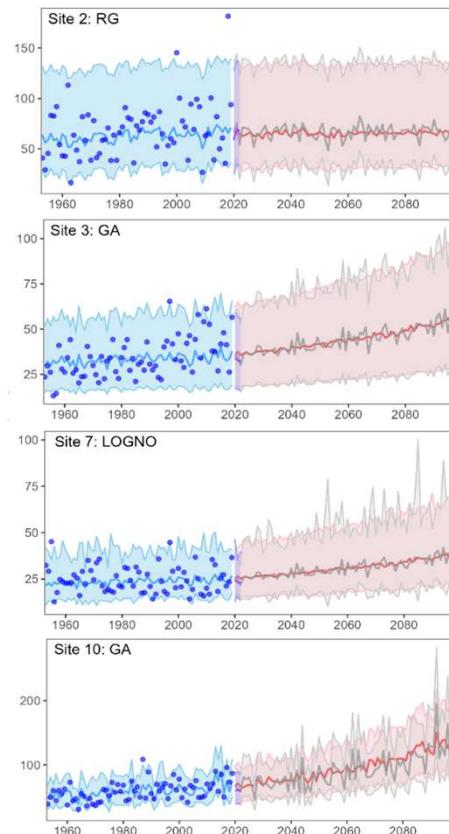


# Results: non-stationary modeling, lagged covar.

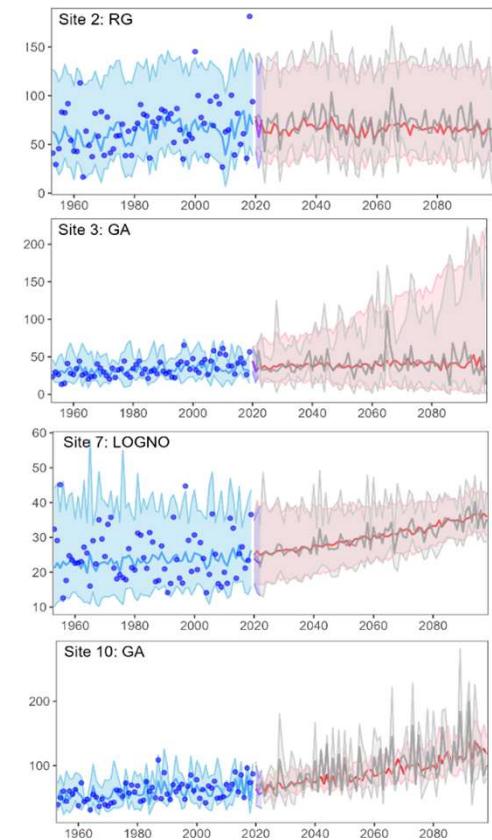
Site	PDF	AIC-S	AIC-NS	DF	Par.	Model structure
2	RG	626.705	615.604	4	$\theta_1$ $\theta_2$	$59.761 + 11.321 \cdot NA0w_1 + 5.937 \cdot EAWRw$ 2.956
3	GA	509.627	500.219	10	$\theta_1$ $\theta_2$	$3.550 + 0.096 \cdot EAw_1 - 0.176 \cdot SCAw_1$ + $cs(NA0w_1, 3)$ $-1.367 - 0.355 \cdot NA0w_1 + 0.242 \cdot EAw$
7	LOGNO	449.596	445.722	4	$\theta_1$ $\theta_2$	$3.170 + 0.077 \cdot EAw$ $-1.378 - 0.223 \cdot EAw_1$
10	GA	557.921	516.951	14	$\theta_1$ $\theta_2$	$4.118 + 0.129 \cdot EAw + 0.056 \cdot NA0w$ - 0.094 · EAWRw + 0.154 · EAWRw <sub>1</sub> $-1.900 + cs(EAWRw, 3) + cs(NA0w, 3)$

- Models with lagged covariates have higher performance than models with non-lagged covariates, but their complexity also increases
- High sensitivity of models in the predictive phase

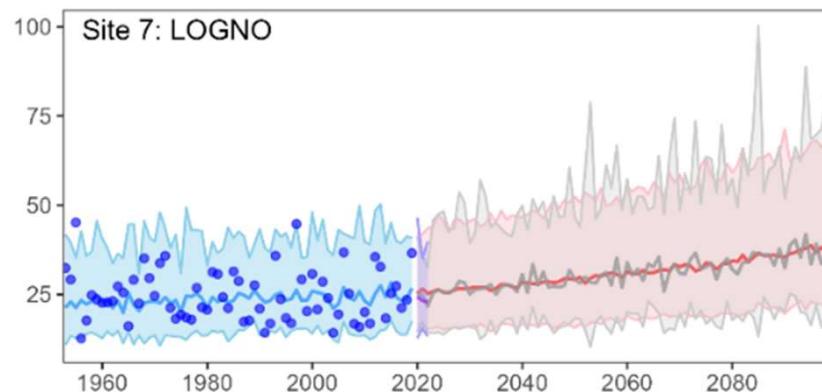
## Non-lagged covariates



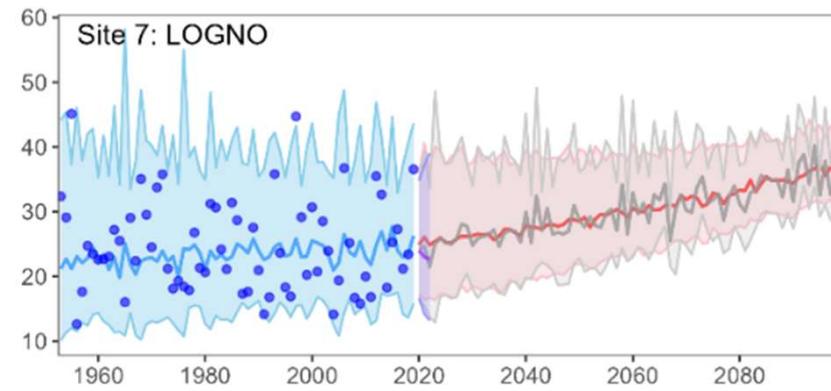
## Lagged-1 covariates



## Non-lagged covariates



## Lagged-1 covariates



Site	PDF	AIC-S	AIC-NS	DF	Par.	Model structure
7	LOGNO	449.596	447.669	4	$\theta_1$ $\theta_2$	$3.180 + 0.081 \cdot EAw$ $-1.339 + 0.239 \cdot SCAw$
7	LOGNO	449.596	445.722	4	$\theta_1$ $\theta_2$	$3.170 + 0.077 \cdot EAw$ $-1.378 - 0.223 \cdot EAw_1$

- Different model structures (see  $\theta_2$ )
- Similar AIC
- Opposite behavior in projected variance (?)

Which model do I select?


 Equifinality

- AMDP over several Spanish regions are experiencing some deviation from the stationary assumption (change points and trends)
- Non-stationary modeling revealed serious problems that led to doubts about the reliability of the adopted models
  - Equifinality makes it difficult to select a representative non-stationary model
  - There is uncertainty associated with extrapolating the relationships between distribution parameters and covariates into the future, as these relationships may change as the sample data increase
- There are no projections for all climate indices
- **We need to find a physical mechanism to explain non-stationarities**



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# Thank you for your attention!

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Bridging the gap between water science and solutions – A joint conference  
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